Delay Performance of Different Train Types Under Combinations of Structured and Flexible Operations on Single-Track Railway Lines in North America

Darkhan Mussanov a, 1, Nao Nishio a, C. Tyler Dick, PE a
a Rail Transportation and Engineering Center (RailTEC), Department of Civil and Environmental Engineering, University of Illinois at Urbana-Champaign 205 N Mathews Ave, Urbana, IL 61801, USA
1 E-mail: mussano2@illinois.edu, Phone: +1 (217) 244 6063

Abstract

North American freight railroads typically operate flexible train schedules where train dispatchers resolve train conflicts in real-time. This is in contrast to Europe, Asia, or rail transit networks where structured train operations follow a pre-planned timetable. Under flexible operations, trains are dispatched as needed, making it an ideal approach for low-cost transportation of bulk commodities. Recently, North American railways have experienced a substantial decline in demand for bulk transportation of coal. However, demand for premium intermodal traffic that must operate on more rigid schedules has reached record levels. To handle both types of traffic efficiently, North American railways are faced with the challenge of operating both flexible and structured train schedules on the same route infrastructure. This paper seeks to understand how different combinations of scheduled and flexible trains, the amount of schedule flexibility, and train priorities impact the performance of a single-track rail corridor. Rail Traffic Controller (RTC) simulation software was used to simulate different operating conditions for a fixed traffic volume on a representative rail corridor. The results suggest that efforts to reduce delay and improve level-of-service by reducing schedule flexibility show little return until operations become highly structured with little flexibility. Scheduled trains perform best when there are fewer flexible trains on the route while flexible trains are relatively insensitive to traffic composition. Assigning priority to scheduled trains causes the overall average level-of-service to deteriorate. These general trends can help practitioners plan for operation of different scheduled and flexible train types on the same rail corridor.

Keywords
Scheduling, flexible operations, train delay, simulation, priority

1 Introduction

North American freight rail traffic reached a peak in 2006 on the strength of heavy haul transportation of bulk commodities and double-stack containers in international trade (FRA (2015)). Following three years of traffic declines due to economic recession, freight rail traffic has slowly returned to 2006 levels. However, the composition and geographic distribution of this traffic has substantially changed. Coal traffic has declined by over 20 percent since 2006 while intermodal traffic has reached record levels (AAR (2016)). Domestic package delivery companies have driven the growth of domestic intermodal
traffic by contributing premium traffic that requires predictable service on precise schedules. At the same time, there has been strong public and agency interest in expanding commuter and regional intercity passenger rail service on these same freight corridors. Thus many rail corridors are experiencing a transition from bulk freight trains operating on flexible schedules to maximize efficiency and economies of scale, to premium services that require more structured operations with fixed arrival and departure times. Although, passenger, commuter and premium intermodal trains receive higher priority on the shared corridors compared to bulk and manifest traffic, maintaining the schedule flexibility of bulk freight trains while simultaneously providing the precision and level-of-service required by passenger and intermodal trains presents a substantial operational challenge on the predominantly single-track North American rail network.

To help increase the level-of-service of a single-track railway network with different train types, railways may add passing sidings (passing loops), extend siding lengths, and add double track. These actions can increase line capacity, reduce delay or allow for more flexible operations but the infrastructure projects are capital intensive and each railroad needs to maximize their return on infrastructure investment. Understanding the capacity and level-of-service impact of altering the number of trains that depart precisely with the timetable and according to flexible schedules can aid practitioners in evaluating operating plans and potential infrastructure investments.

This paper seeks to understand how different combinations of scheduled and flexible trains impact the performance of a single-track rail corridor. Simulation experiments were conducted to examine how increasing the number of flexible trains within baseline traffic of all scheduled trains alters the performance of a representative rail corridor. The results of the experiments provide a better understanding of the fundamental relationships between the proportion of scheduled and flexible trains, amount of schedule flexibility, and train delay. The findings of this paper are not intended to suggest that one type of operation is better than the other but rather to help practitioners consider the interaction of flexible and scheduled trains in evaluating line capacity and infrastructure investment.

2 Background

Railway operations can be classified into two broad types: scheduled and flexible (Figure 1). Under scheduled operations, all of the trains in the network depart according to a pre-planned timetable with a fixed departure time and fixed arrival time (Figure 1a). The timetable is constructed such that any conflicts between trains are resolved and if the same timetable is executed each day, the same trains will meet and pass at the same locations each day. This kind of operation is very common in passenger and transit networks and railways in Europe and Asia. Precise operation according to a rigid timetable has also been termed structured operation (Martland (2009)).

Under flexible operations, trains do not have a fixed timetable and depart terminals as needed or within a range of pre-determined departure times. Most North American freight trains are operated in this manner, with train dispatchers routing the trains and resolving conflicts in real-time (Sogin (2013a)). Since train meets and passes occur at different locations each day, the running time of individual trains can vary greatly. Thus flexible trains, also referred to as unscheduled trains, exhibit both flexible departure times and flexible running times over the route (Figure 1b and 1c). The result is that flexible trains have variable arrival times at terminals or the ends of route segments under study.
The traffic on a given rail corridor may include both scheduled and flexible trains. A route with a combination of scheduled and flexible train operations is referred to as heterogeneous traffic. If all trains on a given route operate in the same manner (i.e. all scheduled or all flexible), the rail traffic on this corridor is known as homogenous traffic. This research focuses on the impact of traffic composition and schedule flexibility under heterogeneous traffic.

Previous research on the impact of schedule flexibility on homogenous traffic with different amounts of route infrastructure was conducted by Dick and Mussanov (2015). The study revealed that when all trains operate with the same amount of schedule flexibility, the train delay response penalty became increasingly insensitive to flexible operation as the amount of schedule flexibility increased. After a certain magnitude of schedule flexibility is reached, there is little change in the level-of-service on the corridor as measured by average train delay.

Other previous research on similar single-track mainlines revealed the concave relationship between train speed heterogeneity and train delay where delay is highest on corridors with a combination of train speeds (Dingler (2009)). This finding suggests that routes with a combination of structured and flexible trains may be more capacity-constrained than routes with heterogeneous train operations. Dingler (2010) also found that the level-of-service on a corridor was impacted when a train with lower priority was moved into a siding to accommodate complex meets between priority trains. Although, this research did not include flexible departure times, the findings suggest that train priority may play a role in the relative delay performance of scheduled and flexible trains. Further support of this hypothesis is suggested by Sogin et al. who found that speed and priority differentials within heterogeneous traffic decrease mainline capacity (Sogin (2013a)). When meets are not perfectly timed with the location of passing sidings, waiting time drives the delay response for trains with lower priority. Setting train priorities increases heterogeneity in the simulation and deteriorates the level-of-service.

Under structured operations, the UIC 406 timetable compression method for capacity evaluation can be applied to both double and single-track lines (Landex (2009)) including passenger corridors in the North American context (Pouryousef (2015)). However, it has been demonstrated that train schedules designed to optimize capacity through this evaluation approach can become susceptible to unexpected delays and disturbances (Larsen...
Thus simulation is most often used to evaluate capacity under the flexible operations found on most North American rail corridors (Pouryousef (2013)). Although heterogeneity in train speed, priority and vehicle capability has been extensively studied, these investigations did not consider the differing schedule flexibility and level-of-service requirements of multiple types of trains. To fill this knowledge gap and aid railway practitioners in planning operations and infrastructure, this research investigates the behavior of routes with combinations of trains exhibiting differing amounts of terminal departure time variability, ranging from precise schedules to complete flexibility. This research seeks to characterize the relationship between the mixture of scheduled and flexible trains operating on a rail corridor, the amount of schedule flexibility in the train departure times, and the level-of-service (train delay) experienced by each type of train.

3 Methodology

To understand the impact of dispatching two different types of railway operations on a typical North American single-track corridor, multiple traffic scenarios were simulated on a representative rail corridor with Rail Traffic Controller (RTC) simulation software.

3.1 Rail Traffic Controller (RTC)

RTC is an industry-leading railway simulation software commonly used by major North American railroads and consultants to assess line capacity and aid decisions on infrastructure investments. Unlike many other railway simulation platforms, RTC does not require a fixed timetable with resolved train conflicts. RTC realistically models the actions of a human train dispatcher in resolving meet and pass conflicts between trains. RTC can also account for schedule flexibility by randomly departing trains within a given range of departure times. For example if the schedule flexibility for a train is specified as 60 minutes, RTC will randomly dispatch the train anytime within 60 minutes before or after the initial set departure time during each day of the simulation. Scheduled trains with no flexibility depart the terminal at the same exact time each day. Each simulated day contains a different random combination of flexible train schedules along with the trains operating on fixed schedules, resulting in differing amounts of train delay. The train delay output is averaged over multiple days of simulated operations and normalized by total train-miles to assess the performance of the traffic scenario.

To determine the number of simulation runs required to obtain a stable train delay response for a given traffic scenario, an initial scenario was simulated for multiple days of train operations and then replicated 100 times using different seeds to randomize the train departures. Average train delay values stabilized after seven replications. Based on this result, each traffic scenario was simulated with RTC for five days of train operations and replicated ten times with different random seeds. The ten iterations provide 50 days of train operations for calculation of the average train delay response associated with a given traffic scenario in the experiment design and plotted as a single data point in the results.

3.2 Baseline Schedule and Introduction of Schedule Flexibility

For use with all of the simulation experiments, a typical North American single-track route was constructed in RTC. The route is 386 km in length and features passing sidings that are 3.22 km long and spaced at 64 km intervals. With the exception of schedule flexibility and
priority, all of the trains in the simulations have identical characteristics based on typical North American freight trains with 115 railcars and three locomotives.

Before introducing flexible trains, a fixed baseline schedule for structured operations was developed. The baseline schedule includes 24 trains per day that depart from either end of the route on even intervals using a return-grid operating model on single track. In order for all of the train meets to occur at the evenly-spaced passing sidings, the train speed, departure interval, passing siding spacing, number of passing sidings and train characteristics (Table 1) were carefully adjusted in RTC until delay was minimized.

Table 1: Baseline schedule parameters

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Length of route</td>
<td>386 km</td>
</tr>
<tr>
<td>Siding length</td>
<td>3.22 km</td>
</tr>
<tr>
<td>Siding spacing</td>
<td>64 km</td>
</tr>
<tr>
<td>Number of sidings</td>
<td>5</td>
</tr>
<tr>
<td>Traffic volume</td>
<td>24 trains per day</td>
</tr>
<tr>
<td>Scheduled departure interval</td>
<td>2 hours</td>
</tr>
<tr>
<td>Maximum speed</td>
<td>37 km/hr</td>
</tr>
<tr>
<td>Locomotive type</td>
<td>SD70 3206 kW, 3 locomotives per trainset</td>
</tr>
<tr>
<td>Train consist</td>
<td>115 railcars at 125 tons each; 2.07 km total length</td>
</tr>
<tr>
<td>Operating protocol</td>
<td>CTC 2-block, 3-aspect</td>
</tr>
</tbody>
</table>

The train paths defined in the baseline schedule were used as the basis of the other traffic scenarios (Figure 2). Scheduled trains always depart in one of these fixed train slots. To introduce schedule flexibility, depending on the desired traffic composition, an even number of scheduled trains is replaced by flexible trains (e.g. four flexible trains replace four of the 24 scheduled trains while the remaining 20 scheduled trains maintain their fixed baseline departure times).

![Figure 2: Replacement of scheduled trains in the initial fixed baseline schedule with flexible trains exhibiting departure time flexibility](image)

After introducing a given number of flexible trains, the variability of the departure times was changed according to the experiment design. For a given traffic scenario, all of the flexible trains are assigned the same value of schedule flexibility. The schedule flexibility is assigned in RTC by inputting a time (± minutes) that defines a departure time window
around the corresponding departure time in the initial baseline schedule. During each simulation day, a train will be dispatched at a random time within the departure time window according to a uniform distribution. For this reason the headways are constantly changing in the system. The experiment design section of this paper provides more detail on the simulated factor levels of schedule flexibility and traffic composition.

In addition to schedule flexibility and traffic composition, another set of RTC simulations were conducted to determine the level-of-service impact of assigning higher priority to all of the scheduled trains.

### 3.3 Experiment Design and Outputs

The experiment design included three variable factors: traffic composition, schedule flexibility and priority level. Each factor was simulated over a range of values or “levels” (Table 2) in a full-factorial design. Simulating all factorial combinations of the factor levels was necessary to capture the non-linear response of delay to each factor.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Values</th>
</tr>
</thead>
<tbody>
<tr>
<td>Traffic Composition</td>
<td>0, 4, 6, 10, 12, 14, 18, 20, and 24</td>
</tr>
<tr>
<td>(% of flexible trains out of 24 trains)</td>
<td>0%, 17%, 25%, 58%, 50%, 58%, 75%, 83%, and 100%</td>
</tr>
<tr>
<td>Schedule Flexibility</td>
<td>0, 10, 30, 60, 120, 180, 240, 300, 360, 420, 480, 540, 600, 660, and 720</td>
</tr>
<tr>
<td>Priority Assignment</td>
<td>Equal Priority or Unequal (scheduled trains have higher priority)</td>
</tr>
</tbody>
</table>

Traffic composition quantifies the number of flexible trains operating on the route. This factor can be expressed as the number of scheduled trains replaced by flexible trains per day or as the percent of all trains on the route that operate on flexible schedules. The number of flexible trains ranges from zero for the case of structured operations (all trains are scheduled) to 24 for purely flexible operations (all trains are flexible). The traffic composition factor is limited to even values to ensure an equal number of flexible trains operate in each direction. In selecting scheduled trains to replace with flexible trains, care is taken to evenly distribute them throughout each day (Table 3). As the traffic composition is changed by increasing the number of flexible trains, the schedule slots taken by flexible trains in the previous traffic compositions are maintained.

As described earlier, the schedule flexibility factor establishes the range of departure times for each flexible train relative to the baseline schedule. The schedule flexibility factor level of zero minutes corresponds to the structured baseline schedule with no deviation in departure time. For higher factor levels, the departures of the flexible trains are randomized over increasingly larger windows up to ± 720 minutes (±12 hours). At this highest factor level, flexible trains depart each terminal randomly within each 24-hour period in a purely unscheduled operation.

The priority assignment factor has two options that determine the relative priority of the
flexible and scheduled trains. For equal priority, all scheduled and flexible trains are assigned the same priority within RTC. For unequal priority, the scheduled trains are assigned a higher priority value relative to flexible trains. This combination is of particular interest since scheduled trains are likely to have higher level-of-service requirements compared to flexible trains.

Output from the RTC simulations is reported as average train delay in minutes per 161 train-km (or 100 train-miles). This unit is very commonly used in the North American railway industry to measure the level-of-service and define line capacity according to a minimum acceptable delay level. Higher delay implies congestion in the network and poor overall performance (Sogin (2013b)). The train delay output can be calculated as an average of all trains to assess the overall performance of the traffic scenario. The delays experienced by scheduled and flexible trains can also be totalled separately to determine the relative performance of each type of train.

Table 3: Replacement of scheduled trains with flexible trains (denoted by XX) for different traffic compositions

<table>
<thead>
<tr>
<th>Departure Time</th>
<th>0%</th>
<th>17%</th>
<th>25%</th>
<th>42%</th>
<th>50%</th>
<th>58%</th>
<th>75%</th>
<th>83%</th>
<th>100%</th>
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</thead>
<tbody>
<tr>
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</table>

3.4 Types of Train Conflicts

A consequence of traffic comprised of a combination of scheduled and flexible trains is that three different types of train meets are encountered: Scheduled – Scheduled (S-S), Flexible – Scheduled (F-S), Flexible – Flexible (F-F). Examples of each type of conflict can be observed in Figure 2b presented earlier in the paper. The point of intersection between two scheduled trains (solid lines) is a S-S conflict. The F-S conflicts occur when a scheduled train (solid line) intersects a flexible train (area). The diamond shapes in Figure 2b occur at the intersection of two flexible trains (areas) and represent a F-F conflict. The three types of meets have different properties with respect to the range of possible meet times and locations, and possible priority differences between the trains. These properties influence the amount of delay that can be expected from each type of meet. The types of train conflicts will be revisited later in the paper as a possible mechanism to explain the simulation results.
4 Results

Following the completion of all simulation experiments, normalized train delay values for each train type were plotted for the case of equal priority (Figure 3 a-b) and unequal priority (Figure 3 c-d). The traffic composition in terms of the number of flexible trains is plotted on the horizontal axis and the train delay response is plotted on the vertical axis. Each coloured series displays a specific level of schedule flexibility via fitted linear or quadratic trend lines with $R^2$ greater than 0.8. For a direct comparison of scheduled and flexible train delay under each priority rule, see Figure 8 in the Appendix.

Figure 3: Train type delay response by traffic composition and schedule flexibility for a) scheduled trains with equal priority b) flexible trains with equal priority c) scheduled trains with unequal priority and d) flexible trains with unequal priority

4.1 Equal Priority

The train delay for scheduled and flexible trains with equal priority is described by a fan-shaped set of linear relationships for each level of schedule flexibility (Figure 3a and 3b). The linear relationships converge to a point when all the traffic is structured. As the value
of schedule flexibility increases, the level-of-service deteriorates. However, there is a
greater difference in train delay between the scenarios with less schedule flexibility than the
cases with greater schedule flexibility. This follows the previous research that suggested
the delay of flexible operations increases rapidly with small amounts of schedule flexibility
but becomes insensitive to schedule flexibilities in excess of 120 minutes (Dick (2015)).
Flexible trains with schedule flexibility of 10 minutes exhibit slightly improved delay
response slightly compared to higher schedule flexibilities.

As evidenced by the linear trend in Figure 3a and 3b, for a given schedule flexibility,
each introduced flexible train adds an equal amount of average train delay, and the value of
the delay increase varies with schedule flexibility. When flexible trains are first introduced,
the flexible trains experience higher values of delay than the scheduled trains. However, as
the number of flexible trains increases, the delay response for both types of trains converges.
When there are only a small number of scheduled trains operating on a route with many
flexible trains, the delay performance of the scheduled trains is essentially indistinguishable
from the flexible trains.

A possible explanation for this last finding is that with equal priority, train conflicts do
not favor a particular type of train. If a scheduled train happens to arrive at a passing siding
earlier than a flexible train, the scheduled train will be held at the passing siding. This delay
shifts the scheduled train off the baseline schedule grid and it essentially becomes another
“flexible” train. When the number of flexible trains on the line increases, scheduled trains
encounter more F-S conflicts and therefore have a higher likelihood of transforming into a
“flexible” train that is no longer operating in its original schedule slot.

Each of the train delay trend lines in Figure 3a and 3b can be described by slope and
intercept parameters (Table 4). The intercept, $b(SF)$, and slope, $m(SF)$, are both functions
of schedule flexibility, SF. The slope term is essentially the delay contribution of each
flexible train under constant schedule flexibility. The b-intercept for scheduled trains is the
delay under the purely scheduled operation. The b-intercept for flexible trains is delay
gained from the introduction of the first 4 flexible trains. Train type delay, $D(SF,N)$, is
estimated as:

$$D(SF,N) = m(SF) × N + b(SF)$$

where,

$m(SF)$ = Increase in train delay as a function of schedule flexibility

$b(SF)$ = Structured operation train delay as a function of schedule flexibility

$N$ = Number of flexible trains introduced

$SF$ = Schedule flexibility

Table 4: Parameter estimates of train type delay for unequal priority

<table>
<thead>
<tr>
<th>Train Type</th>
<th>Slope (train/minutes)</th>
<th>Intercept (minutes)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Scheduled trains</td>
<td>$0.630 \times \ln(SF) - 1.56$</td>
<td>17.3</td>
</tr>
<tr>
<td>Flexible trains</td>
<td>$0.540 \times \ln(SF) - 1.56$</td>
<td>$2 \times \ln(SF) + 15$</td>
</tr>
</tbody>
</table>

4.2 Unequal Priority

For the case of unequal priority, the response of scheduled train delay takes the shape of a
concave function with a gradually levelling slope that becomes flat as number of flexible trains increases (Figure 3c). The curves suggest two general ranges of interest: a low number of flexible trains in the system (between zero and 12 flexible trains) and a high number of flexible trains (from 12 to 24 trains). With a low number of flexible trains, train delay continues to increase with each flexible train introduced. Replacing six scheduled trains by flexible trains with 120 minutes of schedule flexibility nearly doubles the average train delay. Replacing twelve scheduled trains triple the average train delay. However, after introducing 12 flexible trains and entering the range with a high number of flexible trains, scheduled train delay values become increasingly insensitive to the newly introduced flexible trains.

The delay responses of flexible trains with unequal priority trace a parabolic shape (Figure 3d). The parabola takes a concave up shape for low schedule flexibility data series (between 0 and ± 60 minutes) and becomes concave down with high schedule flexibility (beyond ± 60 minutes).

It is hypothesized that the overall balance between F-F, F-S and S-S train conflict types may help explain the observed results. If the scenario does not feature any flexible trains, only S-S meets are present minimal delay is incurred. As the number of flexible trains is increased, a portion of the S-S conflicts are replaced by F-S and F-F conflicts. Scenarios with more than 12 flexible trains experience a gradual replacement of F-S and S-S meets with F-F conflicts.

When given priority, scheduled trains generally do not incur delay at F-S meets except when meets near the end-of-route terminals. The meets near terminals often cause a scheduled train to move off its assigned schedule slot, leading to mismatched S-S meets further down the train path. Since the chance of terminal meet and associated delay is proportional to the total number of F-S meets, delay for scheduled trains steadily increase until 12 flexible trains are added.

When assigned a low priority, flexible train delay follows the concave up and down patterns. Replacing the first four scheduled trains with flexible trains drives the average delay of the flexible trains to be higher than scheduled trains because of F-S conflicts. As previously mentioned, F-S conflicts are almost always resolved in favor of the higher-priority scheduled traffic and cause substantial delay to the lower-priority flexible trains. The delay values reach a maximum when 12 flexible trains are present. At this point there are an equal number of scheduled and flexible trains on the route and heterogeneity in terms of train priority and schedule is at its maximum. As the number of flexible trains increases further, there are fewer priority scheduled trains and the likelihood of a F-S conflict decreases while the number of F-F conflicts increase. Since both trains in a F-F conflict have equal priority, the expected delay is shared between the flexible and scheduled trains, and average delay begins to decrease.

Each of the train delay trend parabolas in Figure 3c and 3d can be described by a polynomial with three parameters that are functions of schedule flexibility (Table 5). Train type delay, \( D(SF, N) \), is estimated as:

\[
D(SF, N) = a(SF) \times N^2 + b(SF) \times N + c(SF)
\]  

(2)

where,

\( a(SF), b(SF) = \) Increase in train delay as a function of schedule flexibility
\( c(SF) = \) Structured operation train delay as a function of schedule flexibility
\( N = \) Number of flexible trains introduced
\( SF = \) Schedule flexibility
Table 5: Parameter estimates of train type delay for unequal priority

<table>
<thead>
<tr>
<th>Train Type</th>
<th>a(SF)</th>
<th>b(SF)</th>
<th>c(SF)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Scheduled  trains</td>
<td>$-0.024 \times \ln(SF)$</td>
<td>$1.13 \times \ln(SF)$</td>
<td>$20$</td>
</tr>
<tr>
<td>Flexible trains</td>
<td>$-0.068 \times \ln(SF) + 0.02$</td>
<td>$2.14 \times \ln(SF) - 7.48$</td>
<td>$33.6 \times SF^{0.022}$</td>
</tr>
</tbody>
</table>

4.3 Schedule Flexibility and Traffic Composition

By examining the combinations of schedule flexibility and traffic composition that correspond to a given average train delay (level-of-service) in Figures 3a-d, the data can be transformed to illustrate the relationship between traffic composition and maximum allowable schedule flexibility to maintain a given level-of-service (Figure 4a and 4b).

Figure 4: Relationship between number of flexible trains and maximum allowable schedule flexibility to maintain a given level-of-service with a) equal priority  
  b) unequal priority
Both figures suggest an inverse functional relationship between schedule flexibility and number of flexible trains introduced. The amount of schedule flexibility required to maintain the level-of-service is highly sensitive to initial increases in the number of flexible trains. For a priority operation and a 30 minutes per 160 train-kilometres level-of-service, the single-track route with 64 kilometre siding spacing could sustain approximately three flexible trains with 720 minutes of scheduled flexibility. If an operator were to replace an additional scheduled train, the schedule flexibility of all flexible trains must be reduced to approximately to 60 minutes to maintain the desired level-of-service. To provide high levels of schedule flexibility while maintaining a low average train delay (high level-of-service), the number of flexible trains should be limited to three or four trains. However, if an operator already runs flexible traffic with 60 minutes of schedule flexibility, there is an option to convert the rest of the scheduled trains to be similarly flexible without affecting average delay values. If majority of the trains on the line are flexible, increasing schedule flexibility beyond 60 minutes increases delay response drastically. Overall, the results suggest that equivalent delay performance can be obtained from the condition where there are a small number of highly flexible trains or a large number of flexible trains with limited schedule flexibility.

From the perspective of a capacity planner, these results suggest it is possible to maintain a high level-of-service when a majority of the traffic is flexible by operating at very low schedule flexibility levels. However, the level-of-service quickly deteriorates (train delay increases) if externalities and disruptions force the operations to become more flexible.

It is hypothesized that the delay equivalency between few but very flexible trains and many but more structured trains arises from the ability of the flexible trains to recover to the baseline return grid schedule train paths. Flexible trains have a certain probability to fall close to the original return grid path and a chance to recover by meeting a scheduled train. Trains with large amounts of schedule flexibility have a low probability to recover due to their large range of departure times. However, flexible trains with 60 minutes of schedule flexibility have a much higher probability of returning to their original scheduled train path. A small number of trains with a low probability of recovery may exhibit the same delay performance as a scenario with a large number of trains with a higher recovery probability.

5 Discussion

The following sections further expand on the presented results and suggest possible mechanisms behind the observed trends.

5.1 Equal and Unequal Priorities

To better illustrate the effect of a change in assigned priority on the delay responses of scheduled and flexible trains, a direct comparison is made between the train types with equal and unequal priorities for a fixed schedule flexibility of 240 minutes (Figure 5).

When the scheduled and flexible trains are given equal priority and there are few flexible trains, the scheduled trains have the lowest delay. As the number of flexible trains increases, the delay of the scheduled trains converges to the same range as the flexible trains. The scheduled trains become do disrupted by the flexible trains that the train types become indistinguishable.
When the scheduled trains are given priority, they exhibit much lower delays compared to the lower priority flexible trains. Even as the number of flexible trains increases and delay of both train types increases, the scheduled trains are able to take advantage of their priority to exhibit lower delay than the flexible trains.

When the delay of scheduled trains with equal and unequal priorities is compared, the findings are somewhat counter-intuitive. When the scheduled trains are assigned a higher priority, their average train delay actually increases. It is hypothesized that the disproportionate increase in train delay experienced by the flexible trains when they are assigned a low priority effectively adds variability to train running times and the locations of subsequent train meets, decreasing the overall performance of scheduled trains.

![Figure 5: Scheduled and flexible average train delay with equal and unequal priorities for schedule flexibility of 240 minutes](image)

To help evaluate this hypothesis, the percent change in train delay values between the case of equal and unequal priorities was determined for the simulated trains across all experiment scenarios (Figure 6). Positive percent change values indicate improvement in average train delay when priority is introduced while a negative change indicates deterioration in average delay values. The vertical axis represents the percentage of trains experiencing a particular percent change in delay. About 35 percent of scheduled trains do not experience a change in performance when they are given priority.

A series Wilcoxon Rank Sum Tests was performed on the data for both scheduled and flexible train distributions to test the null hypothesis that these two populations are identical. The results give a p-value $= 9.34 \times 10^{-14}$ and at $\alpha = 0.05$, which reject the null hypothesis stating that these populations are identical. Therefore these populations are significantly different.

As priority is assigned to scheduled trains, the performance of flexible trains almost always deteriorates. About 86 percent of flexible trains experience deterioration. It is intuitive that flexible trains have higher delay values in unequal priority operation, since train dispatcher will almost always favor a scheduled train at the conflict point. However, the delay response of scheduled traffic is somewhat mixed. About 44 percent of scheduled
traffic experienced an increase in delay, 23 percent lower delay and 33 percent no change. From the practitioner perspective, these mixed results suggest that introducing priority does not necessarily improve the performance of the high priority traffic. The additional delay accumulated by the lower priority trains can cause further cascading disruptions to some of the scheduled trains and decrease their performance despite their higher priority.

Figure 6: Frequency distribution of percentage delay change subject to transitioning from operation with equal priority to unequal priority for a) flexible trains b) scheduled trains

5.2 Types of Train Conflicts and Delay Mechanics

To further expand on the previous discussion, consider the potential train delays accumulated at F-S meets under operations with equal and unequal priorities (Figure 7). The figure illustrates the different interactions between scheduled trains (blue line) and a flexible train (red line within a shaded red band). There are two conditions that influence the delay arising from the interaction between these two types of trains: flexible train shift from the baseline grid schedule slot and train priority.

If both trains are operated with equal priority, a flexible train arriving early is likely to have its train path delayed back to follow the initial baseline train slot (Figure 7a). The flexible train effectively becomes another scheduled train, reducing or eliminating any delays at subsequent meets with scheduled trains. However, a meet between a scheduled train and a late flexible train with equal priority would force the scheduled train off its prescribed train slot (Figure 7b). Once delayed, the scheduled trains will accumulate additional delays at each subsequent meet with a scheduled train. For the case of equal priority, late flexible trains lead to a deterioration of the level-of-service for scheduled trains, whereas scheduled trains can lead to an improved slot positioning for an early
flexible train.

In the case where scheduled trains are given priority, an early flexible train experiences the same improvement (Figure 7c). However, a late flexible train will encounter large delays while waiting at the neighbouring siding for a meet with the higher-priority scheduled train. There are some cases where the flexible trains happen to reposition into an unused train slot and do not cause additional cascading train delay. However, when capacity utilization is high and all train slots are filled, such repositioning will lead to severe delays that may negatively impact other scheduled trains on the route. This is another possible mechanism to explain why not all scheduled trains experience improved performance when assigned higher priority. A closer siding spacing (lower capacity utilization) may affect the ability of the flexible train to move into an unused train slot and prevent secondary delay. This effect will be investigated in future phases of this research.

![Figure 7: Comparison of potential meet scenarios of opposing flexible and scheduled trains under conditions of a) the flexible train arriving early to the meet location with equal priority b) the flexible train arriving late to the meet location](image)

5.3 Terminal Effects

A unique form of flexible – scheduled conflicts was observed near the terminals at either end of the route. Scheduled trains are sometimes forced to depart late from the terminal and shift from the initial return-grid schedule train slot. This phenomenon occurs when a flexible train has already departed from the last passing siding and is moving towards the terminal at the time the scheduled train is required to depart the terminal. In this scenario, the dispatching logic has no choice but to let the flexible train proceed to the terminal and
delay the scheduled train even if it violates priority rules. Consequently, the scheduled train shifts from its train slot and behaves like a flexible train with a delayed departure.

6 Conclusions and Future Work

For a given constant traffic volume and infrastructure, traffic compositions with various levels of schedule flexibility yield distinct results depending on the assigned train priorities. Operation with equal priorities shows little difference in performance between scheduled and flexible trains. However, operating with unequal priorities yields distinct performance differentials between the two train types. Delay curves with equal priorities show linear trends for both train types; incremental introduction of flexible trains causes similar increases in delay. Delay curves with unequal priorities display a quadratic relationship with level-of-service being proportional to the number of flexible – scheduled (F-S) train type conflicts. Given the infrastructure simulated in this study, operating with unequal priorities yields mixed improvement in the performance of scheduled traffic and strict deterioration for flexible traffic. Scheduled traffic is often delayed from its assigned departure time by inbound flexible trains at terminals, causing the scheduled train to operate like a flexible train and cascade secondary delay down the line.

From a level-of-service perspective, equivalent delay performance can be obtained from the condition where there are a small number of highly flexible trains or a large number of flexible trains each with limited schedule flexibility. From the perspective of a capacity planner, these results suggest it is possible to maintain a high level-of-service when a majority of the traffic is flexible by operating at very low schedule flexibility levels. However, the level-of-service quickly deteriorates (train delay increases) if externalities and disruptions force the operations to become more flexible.

Future work in this area will introduce various levels of infrastructure, traffic volume and initial timetables to provide additional understanding on the trade-off between infrastructure investment, traffic volume, schedule flexibility and initial timetable design. For a given traffic composition and volume, a desired delay level-of-service may be achieved through different combinations of timetable design and infrastructure investment. Operations that isolate flexible trains to specific times of the day and wider slots could be compensated by infrastructure investment.

As discussed above, in the case of 64 kilometre siding spacing operating with unequal priorities yields mixed results for scheduled traffic. Operating preconditions that bring distinct improvement to performance of scheduled traffic could provide planners with a more refined checklist for enhancement of high priority traffic.

The number of F-F, F-S and S-S conflicts seem to govern the overall relationship between traffic composition and schedule flexibility. Quantifying the exact impact of the types of conflicts on the level-of-service is another logical step for future research on this topic.

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Appendix

Figure 8: Train type delay response trends of different combinations of traffic composition and schedule flexibility for a) scheduled trains and flexible trains with equal priority b) scheduled trains and flexible trains with unequal priority

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